

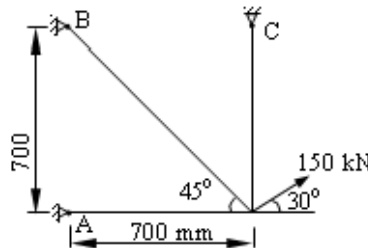
III B.TECH – II SEM EXAMINATIONS, DECEMBER - 2010
FINITE ELEMENT & MODELING METHODS
(AERONAUTICAL ENGINEERING)

Time: 3hours

Max.Marks:80

Answer any FIVE questions
All questions carry equal marks

- 1.a) Derive the finite element equation using the potential energy approach.
- b) Explain the various steps involved in solving a problem using finite element method. [8+8]
- 2.a) Derive an expression relating local and global coordinates.
- b) Explain the advantages of natural coordinates over other coordinates. [8+8]
3. The plane truss shown in figure 1 is composed of members having a square 10mm x 10mm cross section and modulus of elasticity $E = 90 \text{ GPa}$. Compute the nodal displacements in the global coordinate system for the loads shown. Also, compute the axial stress in each element. [16]



- 4.a) State the properties of eigen vectors.
- b) Derive the element lumped mass matrix for a 2-dimensional beam element. [8+8]
5. How do you generate an iso-parametric quadrilateral element for C^1 continuity? Explain with example. [16]
- 6.a) How to evaluate the errors in Gauss quadrature numerical integration? Explain for two points method.
- b) Evaluate the $\int_{-1}^{+1} \left[2x^3 + 4x^2 + \frac{3}{(x+6)} \right] dx$ over the limits -1 and +1 using one point and two point Gauss quadrature methods. [8+8]
7. Prove how an isotropic axisymmetric solid element subjected to axisymmetric loading has effectively a 2-Dimensional state of stress. [16]
- 8.a) What are the current trends in finite element analysis software's? Explain the latest additive modules in ANSYS package.
- b) Explain methodology to consider the loads and boundary conditions over the domain for different types of loads using ANSYS package. [8+8]

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- 1.a) Explain the basic concept of FEM and list some of its advantages and applications.
- b) Explain the principle of virtual work. [8+8]
- 2.a) Explain the natural coordinate system for one-, two- and three-dimensional elements.
- b) Evaluate the natural coordinate ξ , shape function N_1 and N_2 at point P shown in figure 1. If $q_1 = 0.075$ mm and $q_2 = -0.125$ mm determine the value of displacement q at point P. [6+10]

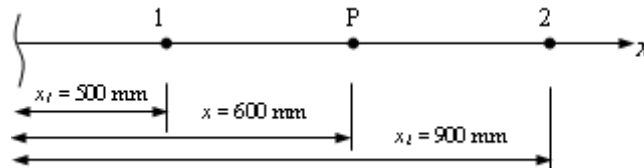


Figure 1

- 3.a) Explain the difference between isoparametric, subparametric and superparametric elements.
- b) Derive the stiffness matrix for a 3-D frame element. [8+8]
4. Find the nodal displacements and strain in element 2 for the truss shown in figure 2. $E=100$ GPa; $A=500$ mm². [16]

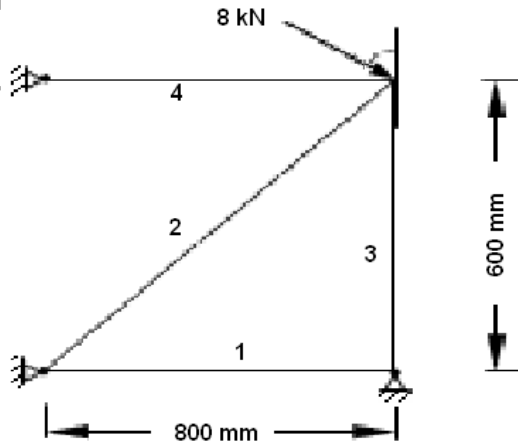


Figure 2

- 5.a) Discuss how the stiffness matrix can be evaluated for Isoparametric elements?
- b) Distinguish between Lagrangian and Serendipity family elements. [8+8]

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SET-2

- 6.a) Explain the one-point Gaussian quadrature method for the numerical integration with suitable example.
- b) What are the approximations and errors associated in one point Gaussian quadrature formula? Explain. [8+8]
7. The nodal coordinates for an axi-symmetric triangular element are $(r_1, z_1) = (20, 10)\text{mm}$, $(r_2, z_2) = (40, 10)\text{mm}$, $(r_3, z_3) = (30, 50)\text{mm}$. Determine the Strain- Displacement matrix for this element. [16]
- 8.a) Explain different methods of mesh generation techniques.
- b) Describe the ANSYS package and its uses in finite element analysis. [8+8]

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- 1.a) Derive the finite element equation using the direct stiffness method.
- b) Explain the various engineering applications of Finite element method and mention the field variable in each application. [8+8]

- 2.a) Derive the relation between natural and global coordinates.
- b) In one-dimensional quadratic element, nodal displacement at i^{th} node is $q_i = 6$ mm and j^{th} node is $q_j = 8$ mm. The displacement at a point P is given as $u = 6.25$ mm and the corresponding shape functions are $N_i = 1/4$ and $N_j = 1/6$. Find
 - i) N_k and
 - ii) nodal displacement at k^{th} node q_k . [8+8]

3. Calculate the nodal temperature using one dimensional heat transfer analysis in a fin (diameter=1 cm, length=8 cm). Using two elements and assuming the tip to be insulated. Base temperature= 100°C , Convection heat transfer coefficient $h=0.1\text{W/cm}^2\text{-}^{\circ}\text{C}$, Thermal conductivity $K = 4\text{ W/cm}^{\circ}\text{C}$ and ambient temperature is $T_a = 30^{\circ}\text{C}$. Comment on the selection of the elements for obtaining accurate solution. [16]

- 4.a) What are the essential and natural boundary conditions in heat transfer problems?
- b) Obtain the eigen values and eigen vectors for the cantilever beam of length 2m using constant mass for translation dof with $E = 200\text{GPa}$, $\rho = 7500\text{kg/m}^3$. [6+10]

- 5.a) Discuss in detail the concept of Isoparametric Element?
- b) Using Isoparametric concept, Formulate the Element Stiffness Matrix for a uni dimensional Two Noded element with constant cross sectional area 'A' and Modulus of Elasticity "E". [8+8]

- 6.a) Discuss the importance of finite element modeling in solving the field problems.
- b) How to store the large scale matrices? Explain with different methods. [8+8]

- 7.a) Derive the Jacobian matrix for 2-D axi-symmetric problems.
- b) Explain the method to simplify the given domain using symmetric boundary conditions with suitable examples. [8+8]

- 8.a) How to generate the regions of mesh generation? Explain with examples.
- b) Explain the methods for specifying the loads and boundary conditions in finite element modeling. [8+8]

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- 1.a) Discuss about equilibrium, compatibility and convergence requirements related to finite element analysis.
- b) Explain about simplex, complex and multiplex elements with respect to degree of freedom. [8+8]
- 2.a) Compute the shape functions at point Q shown in figure 1a using line coordinates.

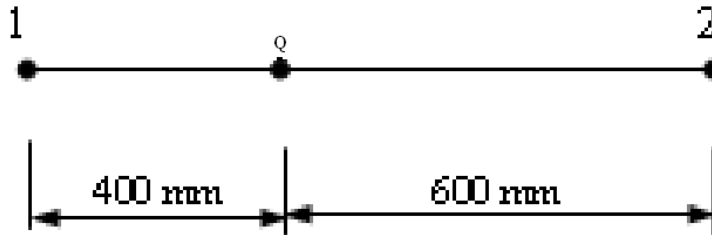


Figure 1

- b) For the triangular element shown in figure 1b obtain the shape functions at point P(2,2) within the element using area coordinates. [6+10]

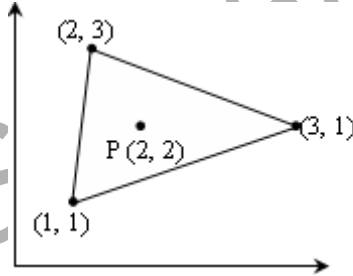


Figure 1(b)

3. Calculate the element stresses for the element shown in Figure 2 for plane stress and plane strain condition when nodal displacements are as given below:
 $q_1 = 0$, $q_2 = 0$, $q_3 = 0.001\text{mm}$, $q_4 = 0.002\text{mm}$, $q_5 = -0.003\text{mm}$ and $q_6 = 0.002\text{mm}$ $E = 200\text{GPa}$, $\nu = 0.25$, thickness = 20mm. [16]

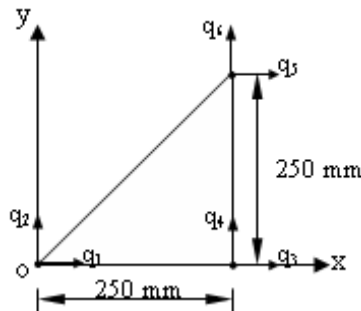


Figure 2

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SET-4

- 4.a) Derive the lumped mass matrix for one dimensional bar element.
b) Derive the stiffness matrix for a 2-dimensional frame element. [8+8]
- 5.a) Explain in detail how the element stiffness matrix and load vector are evaluated in isoparametric formulations.
b) Explain the concept of isoparametric elements and superparametric elements. [8+8]
- 6.a) Differentiate between Simpson's rule and Gauss quadrature.
b) Evaluate the Integral $I = \int_{-1}^1 (2x^3 + 5x^2 + 6) dx$ Using 3 Gaussian quadrature formula. [8+8]
7. Derive the stiffness matrix for 2-D axi-symmetric triangular element from the first principles. [16]
- 8.a) Explain different sub-structuring mesh generation techniques with suitable examples.
b) Compare different commercially available finite element software packages used for heat transfer analysis. [8+8]

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